

# Swaps

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## Interest Rate Swaps

Jonathan Kinlay

# Interest Rate Swaps

- Vanilla interest rate swaps
- Basis swaps
- Amortizing swaps

# Indicative Pricing Schedule

## VANILLA SWAP

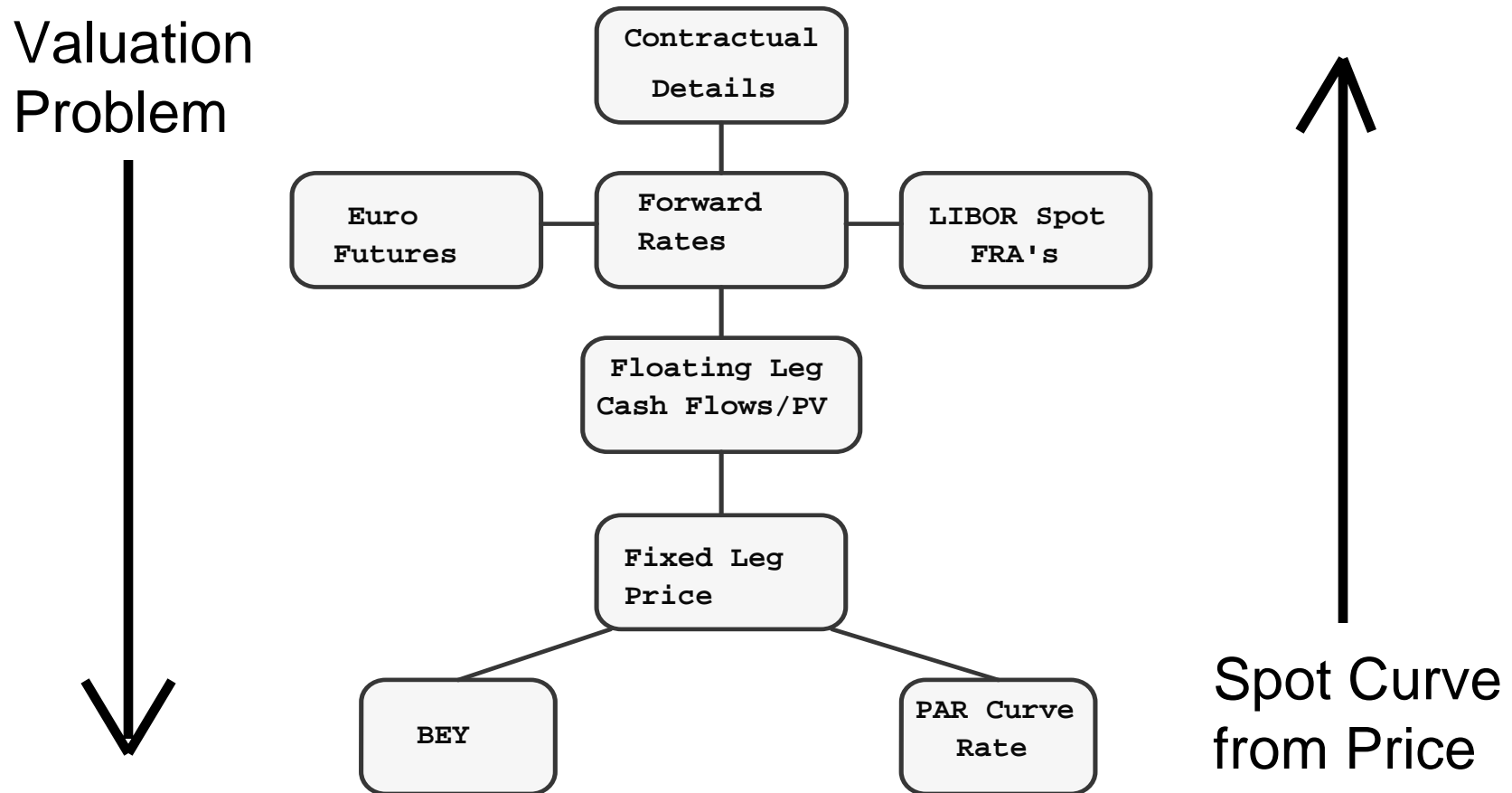
- CITIBANK  
(Reuters: CBSP)
- Monday May 15,  
1999
- Spot Reference --  
USD Libor

1 Year	6.17-22
18 Month	6.19-24
2 Year	6.31-36
3 Year	6.44-49

# One-Year Swap

- Buyer: Pays fixed 6.22 to CITIBANK  
CITIBANK pays 3-Month LIBOR
- Seller: Pays LIBOR to CITIBANK  
CITIBANK pays fixed 6.17
- Spread: 1.25 bps relative to \$100 million  
(approx. \$12,500 per qtr)

# Vanilla: Relation Between Spot Curve and Price



# Vanilla Swap Valuation: Forward Curve Approach

- Two equivalent problems:
  - Given spot curve how do we value/hedge a vanilla swap?
  - Given a schedule of vanilla swap prices what spot curve can we infer?
- Objective: Value the vanilla swap from the spot LIBOR curve

# Lab: Pricing a Fixed for Floating “Vanilla” Swap

Notional principal amount	\$100,000,000
Effective date	September 22, 1994
Day count between each reset date:	
December 22, 1994	91 days
March 22, 1995	90 days
June 22, 1995	92 days
September 22, 1995	92 days
Maturity date	September 22, 1995
Interest settlements are in arrears.	
Fixed Side (Leg):	
Fixed-rate (Swap Coupon)	6.1220%
Compounding frequency	quarterly
Day count	90/360*
Floating Side (Leg):	
Reference Rate	3-month LIBOR
Payment frequency	quarterly resets
Day count	actual/360
First Coupon	5.25%

\* Assumption: Fixed Side Cash Flows Equal over Time

# Key Steps

- Step 1: Project cash flows
  - Contract specifies timing and magnitude of cash flows
- Step 2: Value cash flows
  - Apply time value of money principles

# Step 1: Cash Flow Projections

Quarter	LIBOR	Forward Rate*	Expected Variable Interest**
December	5 1/4	5.25	\$1,327,083
March	5 11/16	6.0496%	\$1,512,395
June	5 15/16	6.2506%	\$1,597,378
September	6 3/16	6.6308%	\$1,694,535

\*LIBOR Forward Rates computed using actual/360 day count.

\*\*Unbiased Expectations

# Step 2: Discounting Cash Flows

- Problem: LIBOR is quoted in an add-on form
- Ignores: Compounding across reset periods
- Objective: Construct the “par LIBOR curve” for discounting LIBOR rates

# Unadjusted Spot Libor Rates: Not the Par Curve

Quarter	Day Count	LIBOR	Forward Rate	E(Variable Int.)	Present Value
December	91	5 1/4	5.25	\$1,327,083	\$1,310,028.80
March	181	5 11/16	6.05%	\$1,512,395	\$1,470,912.00
June	273	5 15/16	6.25%	\$1,597,378	\$1,529,014.70
September	365	6 3/16	6.63%	\$101,694,535	\$95,689,015.90
Total					<b>\$99,998,971.40</b>

\* Including Notional for Expositional Purposes

Fails to equal Notional

$$99,998,971.4 = \frac{1,327,083}{1.0525^{\frac{91}{360}}} + \frac{1,512,395}{1.056875^{\frac{181}{360}}} + \frac{1,597,378}{1.059375^{\frac{273}{360}}} + \frac{101,694,535}{1.061875^{\frac{365}{360}}}$$

# No Arbitrage Restriction

- Net present value must be zero
  - At time of issue the present value of floating rate cash flows discounted back at the floating rate must equal the notional
- What mistake has slipped in?
  - Compounding across reset periods is ignored

# Correcting LIBOR Spots: Effective Annual Yield

## ➤ Spot Curve Correction

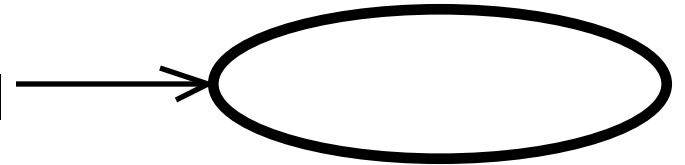
- Adjust for compounding over reset periods

$$1 + {}_0r_m^1 = \left(1 + {}_0r_m \times \frac{\sum \tau}{360}\right)^{\frac{360}{\sum \tau}}$$

$$1.057679 = \left(1 + 5 \frac{11}{16} \times \frac{181}{360}\right)^{\frac{360}{181}}$$

# PV Floating Side

P.V. at EAY = Notional



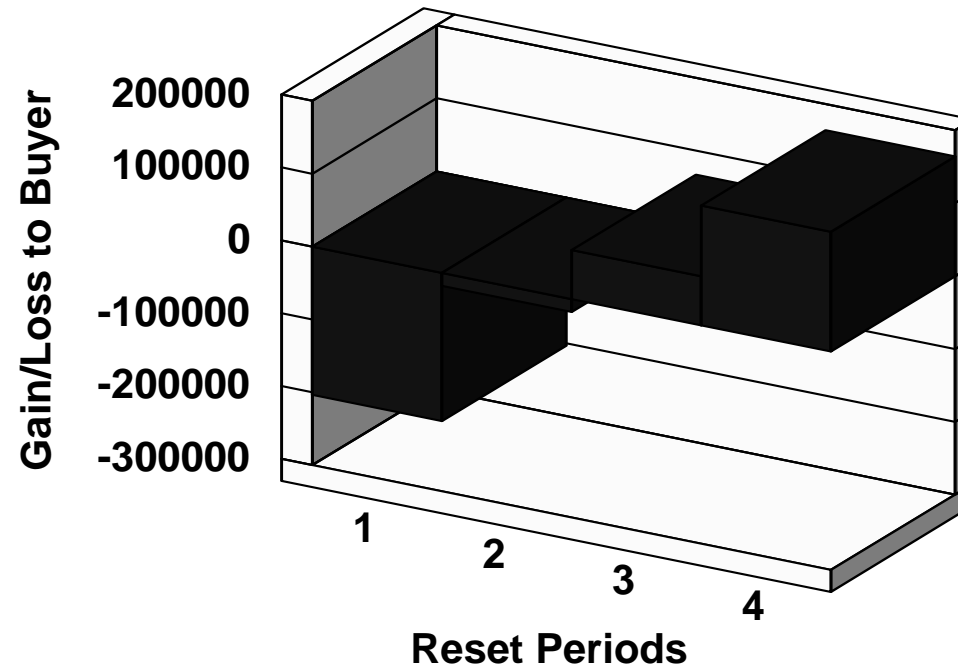
# Fixed Side: Mid-Market Rate

- Fixed side is the Swap Curve
  - Swap rate discounted using “par LIBOR curve”  
= notional principal
  - Equates present value of both legs of the swap
- Computation
  - STEP 1: Swap rate generates future cash flows for fixed leg
  - STEP 2: PV of Cash Flows - Notional

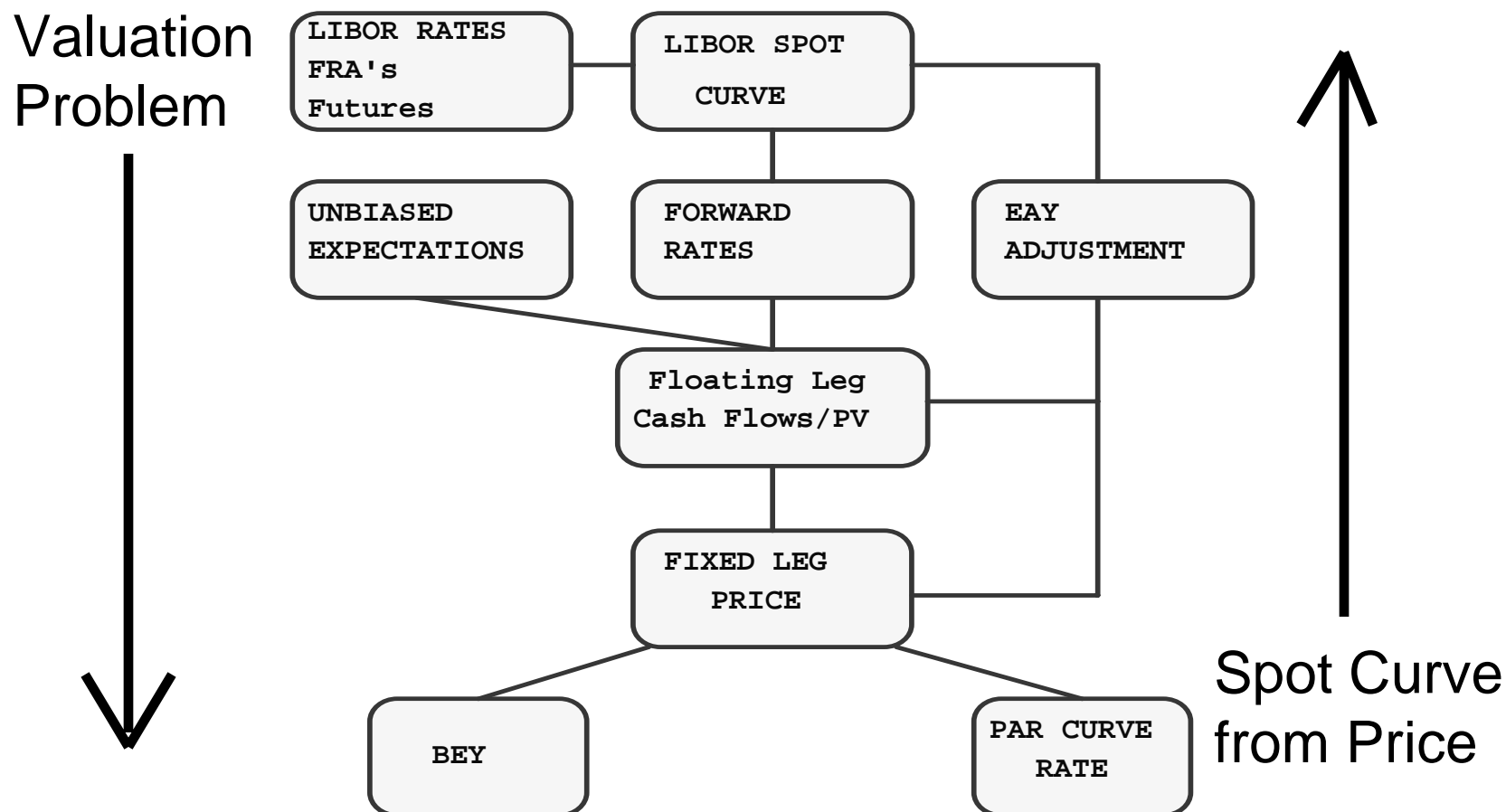
# Swap Price

<b>Qtr</b>	<b>LIBOR Yield Curve</b>	<b>Fixed Interest @ 6.1219933%</b>	<b>Present Value @ EAY</b>
<b>Dec</b>	<b>5 1/4</b>	<b>\$1,530,498</b>	<b>\$1,510,453</b>
<b>March</b>	<b>5 11/16</b>	<b>\$1,530,498</b>	<b>\$1,487,950</b>
<b>June</b>	<b>5 15/16</b>	<b>\$1,530,498</b>	<b>\$1,464,555</b>
<b>Sept</b>	<b>6 3/16</b>	<b>\$101,530,498</b>	<b>\$95,537,042</b>
<b>Total</b>	<b>Both legs exactly equal</b>		<b>\$100,000,000</b>

# Buyer: Net Interest Rate Exposure



# Short Tenor Fixed-for-Floating



# Adjustment for Risk Premium?

- Problem: Forward rate is a biased estimate of expected future spot rate
- Suppose we replace spot curve on floating side with an *expected spot curve*
  - more accurate cash flow projections
  - PV remains unchanged because discount rates also adjust

# Hedging Interest Rate Swaps

- Balanced book
  - Ideal solution
- Hedging problem is relatively simple
  - Eurodollar futures
    - ◆ Problem: marking to market, convexity
  - Strips
    - ◆ Problem: hedge ratio is constant
  - Treasury markets
    - ◆ Problem: TED spread, demand for basis swaps

# Basis Swaps

- First appeared in 1988 --- key building block for any complex structure
- Both cash flow streams linked to floating indices
  - LIBOR/T-Bills
  - LIBOR/CP
  - LIBOR/Prime
- Applications
  - Arbitrage Swap & MM spreads
  - Lock in narrow spreads
  - Switch to responsive index when rates expected to fall

# Basis Swaps: Index Selection

## ➤ TED Spread

- Spread between LIBOR and T-Bills widens when banking industry hits problems
  - ◆ Range 30bp - 130 bp typical
  - ◆ 240 bp in '84 (Continental Illinois), 260 bp in '87 crash

## ➤ Prime-LIBOR Spread

- Should narrow (widen) when s/t rates rise (fall)
  - ◆ Prime is 'sticky' & lags the market driven rates LIBOR

## ➤ LIBOR-CP Spread

- Fell consistently throughout 1980's

# Basis Swap Indices

Index	Quoting Convention	Effective Period
T-Bills	Discount	91 days
CP	Discount	1 month
LIBOR	MMY	6 months
Prime	MMY	1 month

# Basis Swap Quotes (vs. 6-m LIBOR)

	CP/ LIBOR	T-Bill/ LIBOR	Prime LIBOR
2 year	CP+5/1	B+76/59	P-158/165
3 year	CP+6/1	B+86/71	P-150/161
5 year	CP+6/2	B+99/84	P-148/156

- Swap spreads are quoted on a MM basis
  - Yield on T-Bills & CP have to be converted to MM equiv. before spread is added

# Basis Swap Quotes: Fixed Margin over Reference

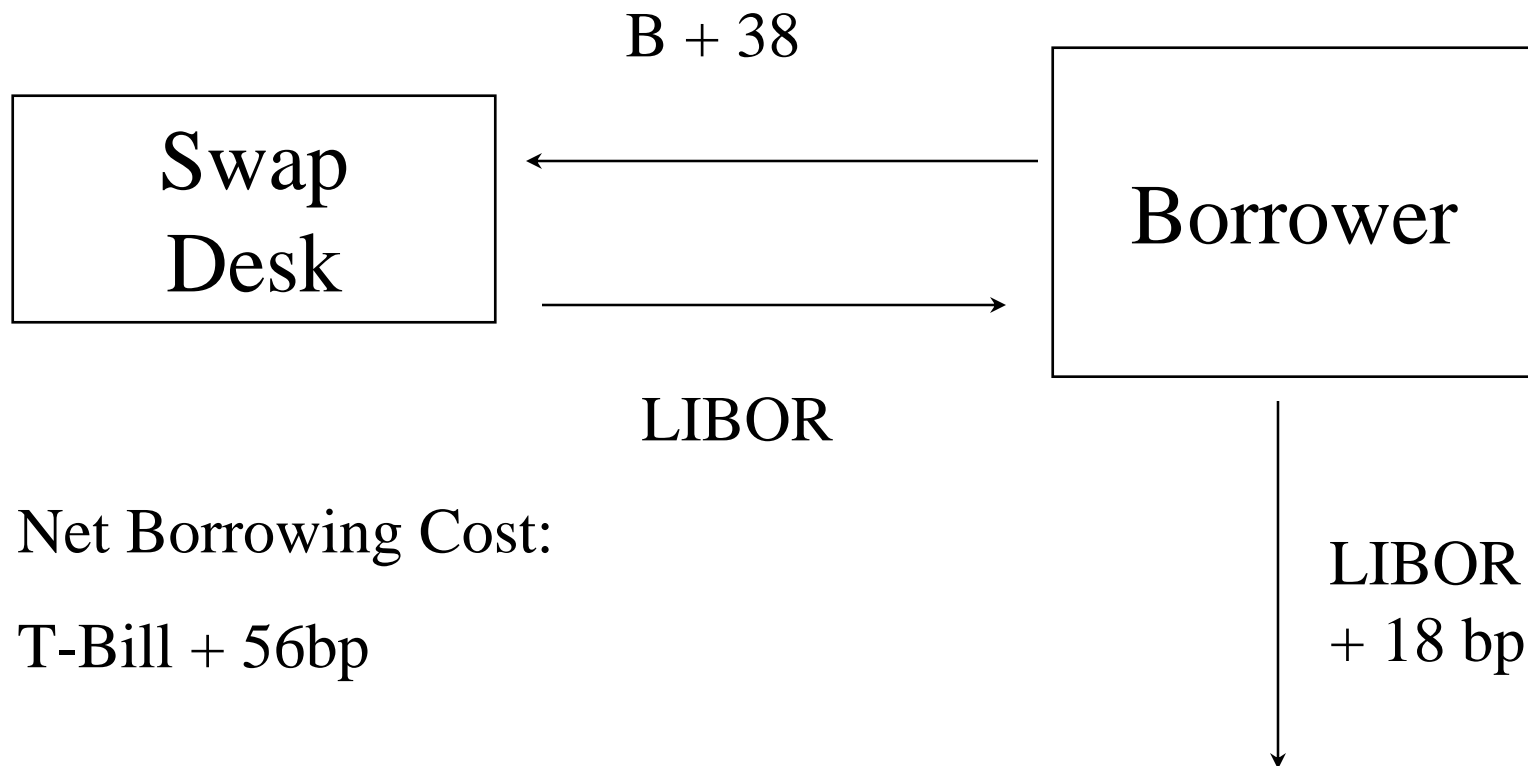
# Interpreting Quotes

- 3-Month: T-bill for LIBOR
- Quote is on a relative basis:
- $B + 32$ ,  $B + 38$
- $B =$  Determined from 3-month auction, converted to MM yield

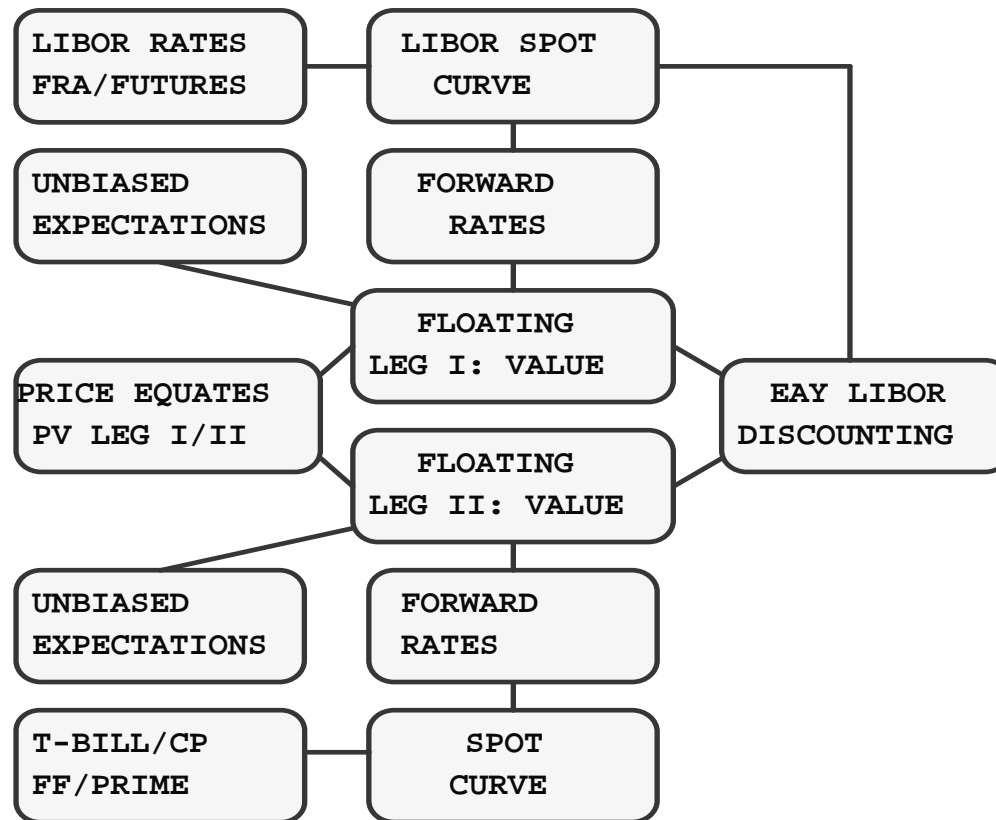
# Trading

- Buyer of T-bill for LIBOR:
  - Pay Desk B+38, Receive 3-month LIBOR
- Seller of T-bill for LIBOR:
  - Gets B+32 from Desk, Pays 3-month LIBOR
- Projected cash flows defined by indexes
- Value both streams from *same* spot curve

# LIBOR- T-Bill Swap Example



# Floating-for-Floating Swaps

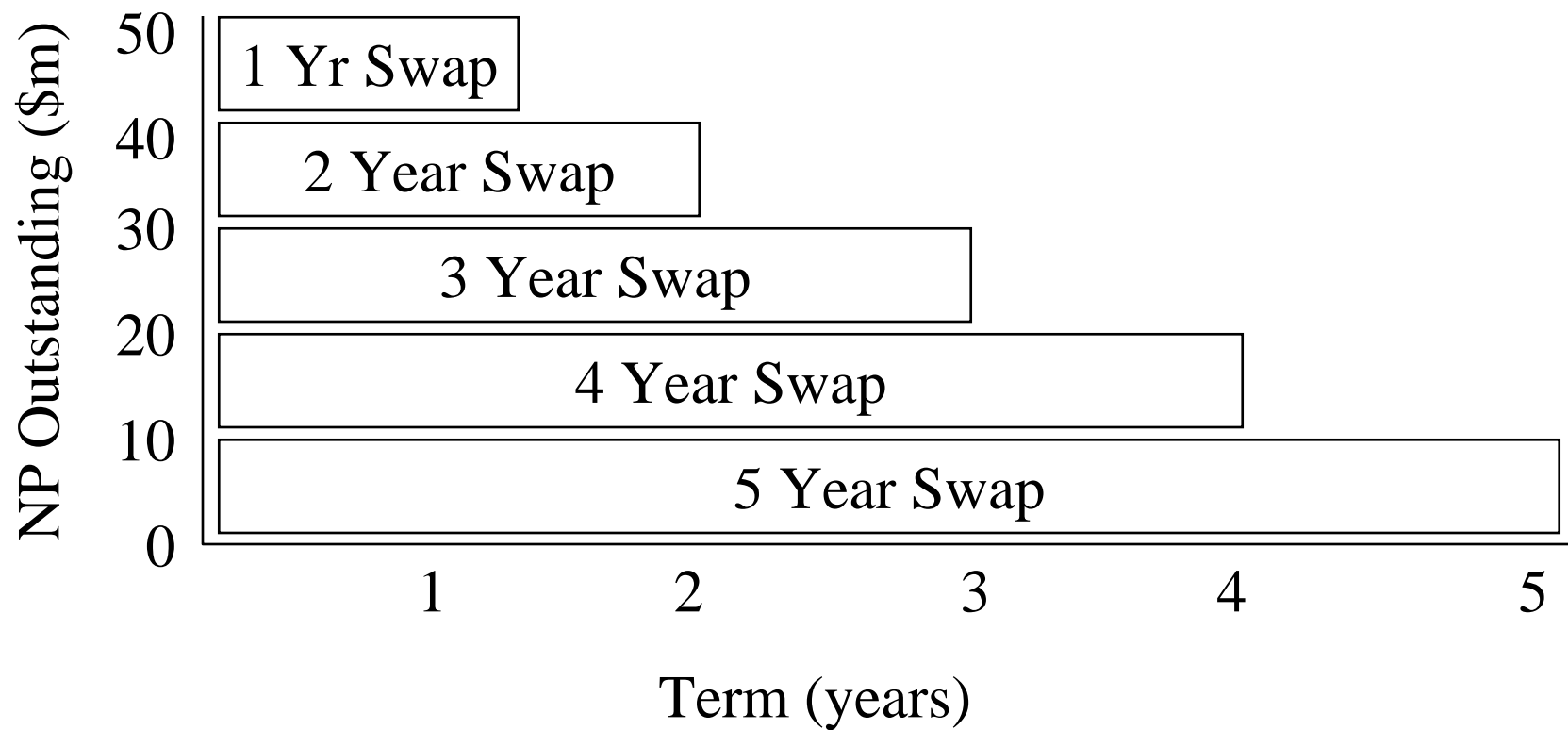


# Amortizing Swaps

- Based on amortizing notional principal
  - Widely used for amortizing loans, lease finance
  - Popular during early 1990's - steep US yield curve
  - “Roller-Coaster”: NP increases *and* decreases
- Analysis of Amortizing Swaps
  - Treat as series of bullet swaps
    - ◆ Compute average maturity, blended swap rate

# Five Year Amortizing Swap Structure

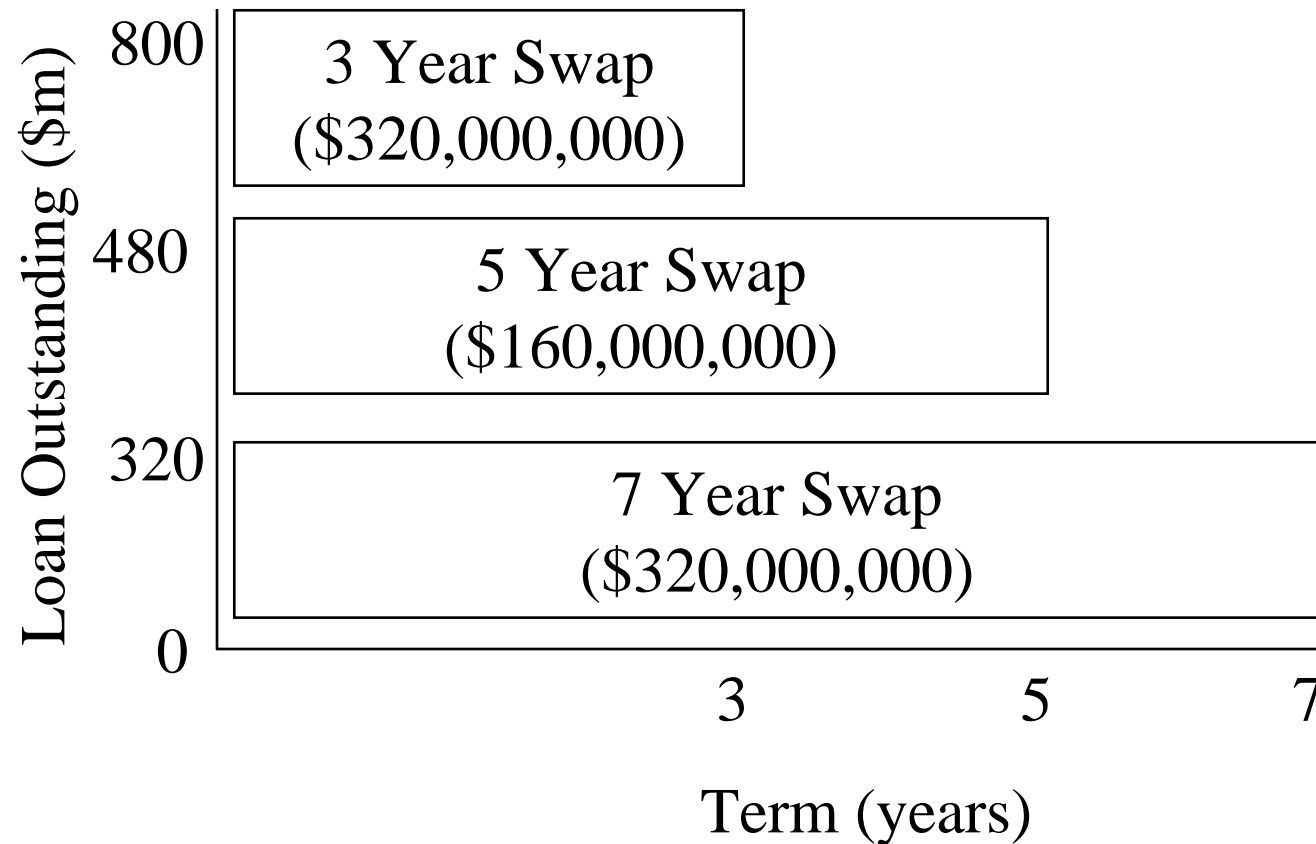
- 5 year swap, \$50m NP, 20% annual amortization



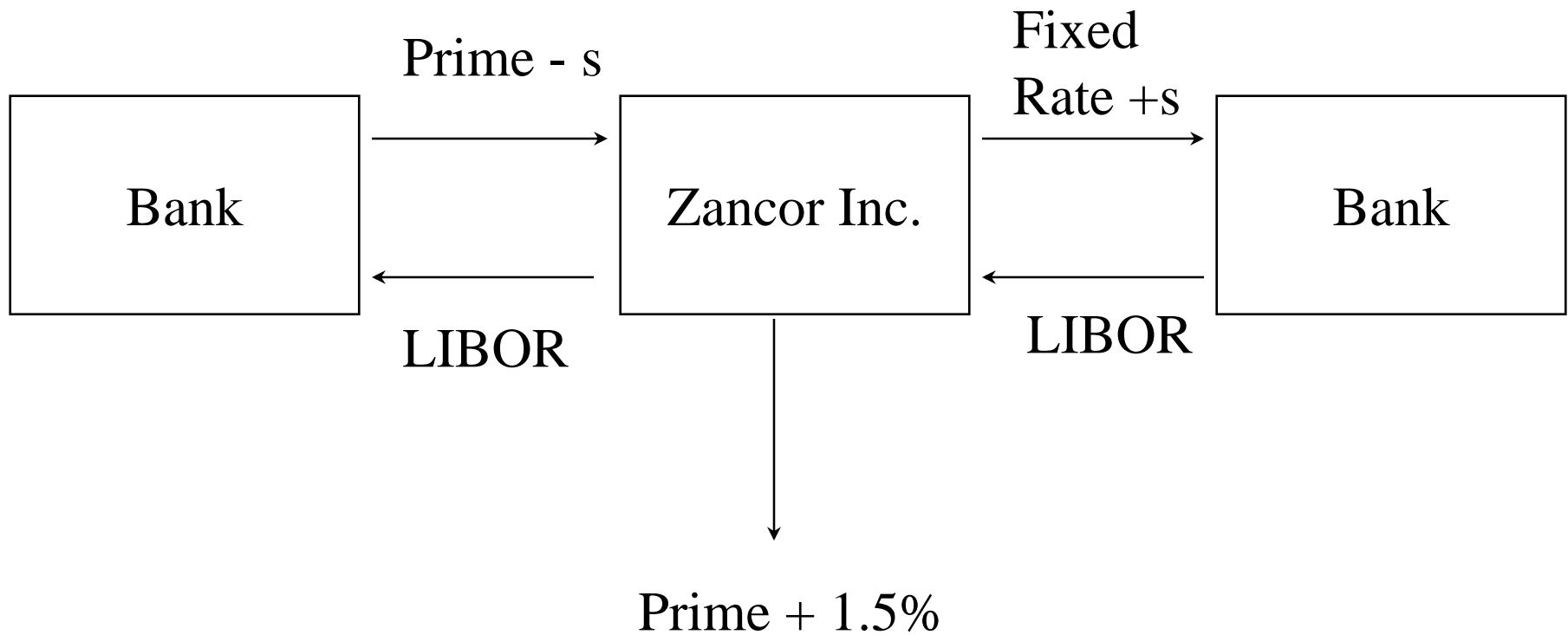
# Lab: Zancor Inc.

- Loan: \$800,000,000 7 year step down revolving credit
  - Price: Prime + 1.5% payable monthly
  - Amortization:
    - ◆ \$320m end year 3
    - ◆ \$160m end year 5
    - ◆ \$320m end year 7
- Client want to swap to fixed rate debt.

# Lab: Zancor Inc. - Amortizing Swap



# Lab: Zancor In. - Swap Structure



# Lab: Zancor Inc. - Swap Rates

Tenor	Treasuries	Coupon Swap	Basis Swap
3 years	5.57%	T+52/57	P-80/-70
5 years	6.01%	T+57/64	P-80/-70
7 years	6.39%	T+55/62	P-80/-70

- Prime is 6.2%
  - Assumed constant

# Lab: Zancor Inc.

- Objective:
  - Find blended swap rate
    - ◆ This is IRR on composite swap cash flows
  - Find all-in loan cost
- Worksheet: Amortizing Swap
  - Workbook: Swaps.xls
  - See written lab notes & solution
  - Also, solution spreadsheet

# Zancor Inc. - Solution

<b>COUPON SWAP</b>	3	5	7
NP	320	160	320
Treasury Rate	5.570%	6.010%	6.390%
Coupon Swap Spread	0.570%	0.640%	0.620%
Credit Fee	0.075%	0.125%	0.175%
Total Fixed Rate	6.215%	6.775%	7.185%

<b>BASIS SWAP</b>	3	5	7
Prime	6.200%	6.200%	6.200%
Basis Swap Spread	-0.800%	-0.800%	-0.800%
Basis Swap Coupon	5.400%	5.400%	5.400%
Loan Spread	1.500%	1.500%	1.500%
Loan Cost	7.700%	7.700%	7.700%

- Blended swap rate: 6.8486%
- All-in loan cost: 9.2250%